



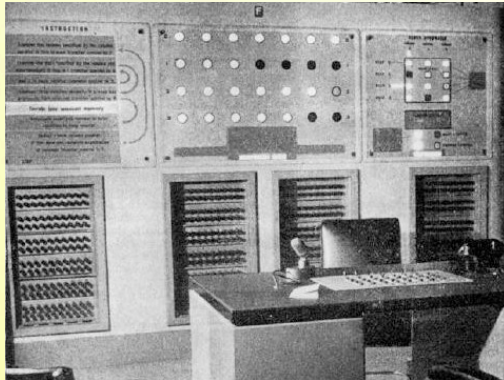
“Welcome to Nimrod” to Learn CS Ideas in the Middle School

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Aarhus, November 11-13

Ferranti NIMROD



Festival of Britain, London, May 1951

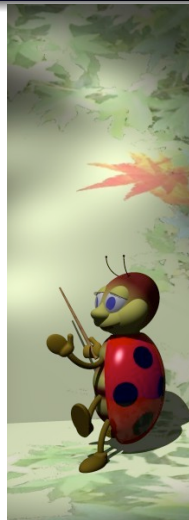


Middle school in Italy

- No separate “informatics” subject
- Some general recommendations in the official programs
- Usually instrumental use of ICT tools (if any)
- Teachers of “Maths and Sciences” have no specific training

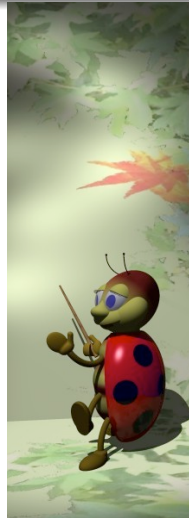
Outline

- 1 Introduction
- 2 Our approach
 - mental processes before concepts
 - computing history in the background
 - cross-disciplinarity
- 3 Welcome to Nimrod
 - program structure
 - coordination of a variety of views
 - roles of history
- 4 Discussion
 - feedback from pupils
 - conclusions



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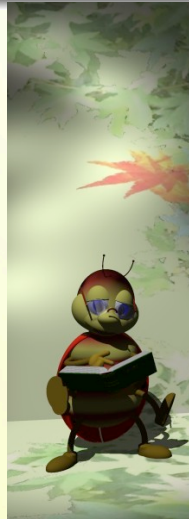
Prelude

“IT mastery is not per se an educational goal [...]

*Informatics is an unceasing quest
to disclose the meaning hidden in a form,
as well as an endeavor
to bind our intended meaning to some form.*

*No one should leave school without (at least)
some appreciation of this about informatics.”*

Charles Duchâteau, 1992

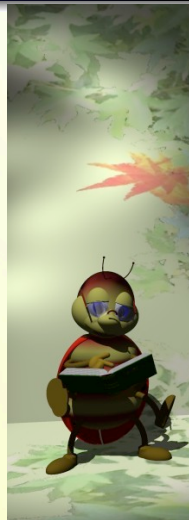


Dexterity with ICTs...

“Direct manipulation interfaces [...] improve the involvement in the operations, but at the price of the illusion that the user can act directly on screen objects, which are based on metaphors [...].

As a consequence, the actual processing cannot be seen and tends to vanish. There is no real mastery, but just some patch-up job without deep understanding. Since the power of CS relies on the opportunity to have a machine do some processing, the illusion of doing directly is definitely a significant obstacle to the mastery as well as to the understanding of the potential of computers”

Éric Bruillard, 2006





... Or intellectual mastery?

- What idea of processing?
- Objective in the long run:
intellectual mastery of information processing tasks
- Development of a *cognitive architecture*



Ingredients of our approach: Mental processes

- emphasis on mental processes rather than concepts
- abstraction from “artifacts” of different nature
- “unplugged” activities with cardboard artifacts
- playful tasks to engage pupils
- history of computing as meta-knowledge for teachers
- themes introduced through (hi-)stories
- abstraction from diverse technologies
- cross-disciplinary links to change teachers' perspective



Ingredients of our approach: History of computing

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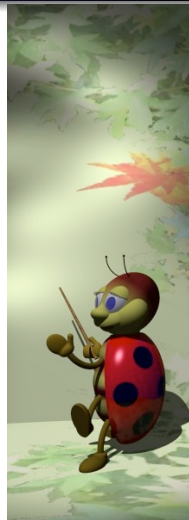


Ingredients of our approach: Cross-disciplinarity

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Inspiring work

- **CS Unplugged**
(e.g.: Bell et al., 2009)
- **CS4FN**
(e.g.: Curzon et al., 2009)
- **Informatik erLeben**
(e.g.: Mittermeir et al., 2010)

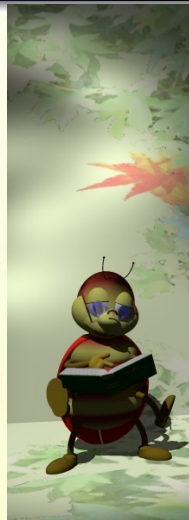


Duval's analysis of mathematics cognition

“From an epistemological point of view there is a basic difference between mathematics and the other domains of scientific knowledge.

Mathematical objects [...] are never accessible by perception or by instruments [...]. The only way to have access to them and deal with them is using signs and semiotic representations.”

Raymond Duval, 2006





Duval's analysis of mathematics cognition

Two kinds of transformations play a central role:

- **treatments**

algorithmic transformations within a semiotic register

- **conversions**

based on mappings between different representations
(cognitively more complex)

The peculiar thinking processes of mathematics require the
cognitive coordination of different semiotic representations



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And what about CS?

treatments – *algorithmic* transformations, Ok. . .

conversions

- basic ideas (information coding, algorithmic processing) are *abstract* in nature, as in mathematics
- CS has constantly to do with mappings between different types of representations of a same entity

Key insights:

it is important to work with heterogeneous representations, including different views of a same algorithmic procedure



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Unplugged computing artifacts

- Duval's semiotic systems can be extended to include all sorts of “glass box” computing artifacts
- Simple “information technology” fully within the pupils' reach (unlike the ICT tools)



Why history of computing?

History of a discipline as . . .

- *repertory* of events to be introduced in a narrative register
- *meta-knowledge* to reflect on instructional methodology



Why history of computing?

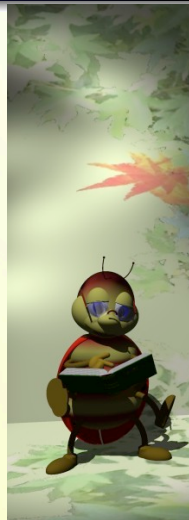
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History as meta-knowledge

“The history of mathematics may be a useful resource for understanding the processes of formation of mathematical thinking, and for exploring the way in which such understanding can be used in the design of classroom activities.”

Luis Radford, 2002



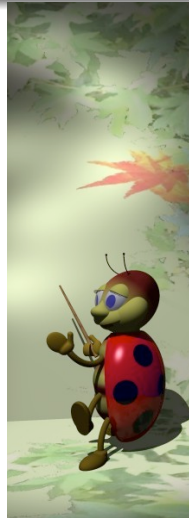


Cross-disciplinarity

- Lower-secondary *informatics* is not a separate subject
- A cross-disciplinary approach to computing is both a need and an opportunity. . .
- . . . helpful to the teachers: unusual CS perspective
- and to the pupils: more critical attitude toward ITs

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“Welcome to... NIMROD” 50 years later

*“This is the first digital computer designed specifically to play a game
— truly the very first Computer Game...*

In the process, it illuminates principles of binary arithmetic and digital logic.

So, leave Lara Croft and her friends behind for a while, and journey back to the years BT (Before Transistors), where just to see a computer is an adventure...”

Pete Goodeve, 2001—





“Welcome to Nimrod” in the middle school

- Core module of about 20 hours of class work
- Additional material for a further 20 hours
- Work still in progress. . . the teachers are trying to ensure continuity to this experience with their classes



Core module

Units

Activities

I. Festival of Britain,
London, May 1951

II. Bits and strategies

III. Magic tricks with bits

IV. Algorithmic procedures

1. A new game to learn

2. Nim player imitation game

3. Brainstorming

4. Snippets of computing history

5. Cross-disciplinary bridges

Survey, questionnaire, test



Extended program

Units

Activities

V. Surprising power
of bit manipulation

VI. Bird's-eye view
of a general procedure

6. Glass-box technology
7. Variations on the “*nim*” theme

8. A bit of philosophy

Review test



Extended program

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Units and activities:

More details in the paper...

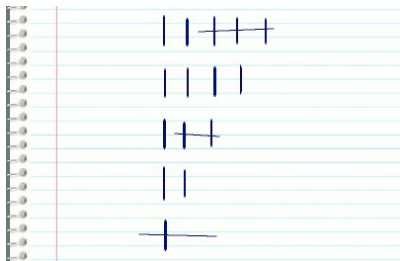
Cognitive coordination of diverse representations

- **Activity 1**
A new game to learn
- Unit II
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Glass-box technology



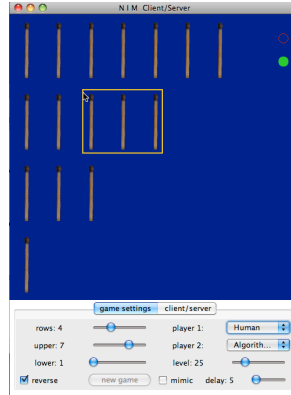
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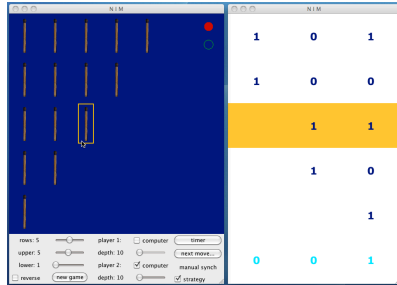
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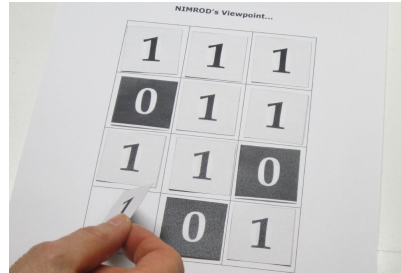
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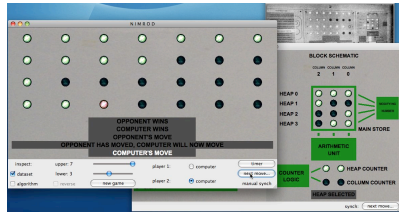
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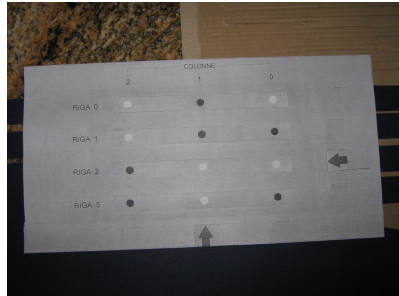
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Different views of an algorithmic procedure

- Unit II
Bits and strategies

||||| 10 = 8 + 2
||||| ← 7 = 4 + 2 + 1
||||| 9 = 8 + 1
|| 2
||| 3

1010 11010
 111 010
1001 → 1001
 10 10
 11 11

0101 0000

- Unit III
Magic tricks with bits

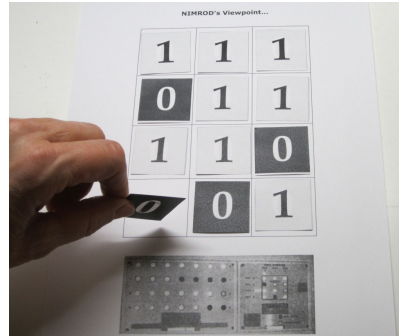
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Algorithmic procedures

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- Unit VI
Bird's-eye view of a general procedure

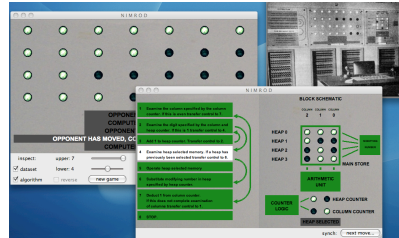
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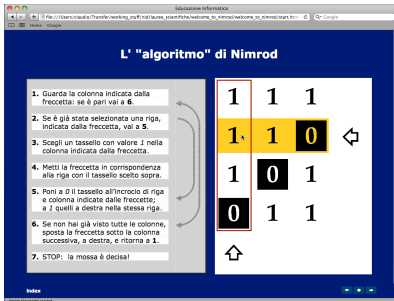
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L' "algoritmo" di Nimrod

1. Guarda la colonna indicata dalla freccetta; se è pari vai a 6.
2. Se è già stata selezionata una riga, indicata dalla freccetta, vai a 5.
3. Scegli un tassello con valore J nella colonna indicata dalla freccetta.
4. Metti la freccetta in corrispondenza alla riga con il tassello scelto sopra.
5. Poni a 0 il tassello all'incrocio di riga e colonna indicate dalle freccette; a J quelli a destra nella stessa riga.
6. Se non hai già visto tutte le colonne, sposta la freccetta sotto la colonna successiva, a destra, e ritorna a 1.
7. STOP: la mossa è decisa!

1	1	1
1	1	0
1	0	1
0	1	1

Navigation icons: back, forward, search, etc.

Different views of an algorithmic procedure

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1. Guarda la colonna indicata dalla freccetta: se è pari vai a 5.
2. Se è già stata collocata una freccetta per indicare la riga scelta vai a 5.
3. Copi un bit con valore 1=bianco nella colonna indicata dalla freccetta.
4. Colloca una freccetta delle righe in cui hai scelto il bit con valore 1=bianco.
5. Sposta a destra il cursore della riga scelta finché nella colonna indicata dalla freccetta compare 0=nero.
6. Se non hai già visto tutte le colonne, sposta la freccetta alla colonna successiva, a destra, e torna a 1.
7. STOP

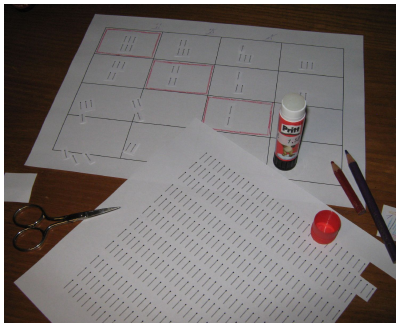
IL GIOCATTORE HA VINTO
IL COMPUTER HA VINTO
IL GIOCATTORE HA SCELTO, TOCCA AL COMPUTER
TURNO DEL COMPUTER

SCHEMA A BLOCCHI
COLONNA 2 COLONNA 1 COLONNA 0
RIGA 0
RIGA 1
RIGA 2
RIGA 3

UNITÀ ALGEBRICA
 CONTINUA PAGA
 CONTINUA COLONNA
RIGA SELEZIONATA

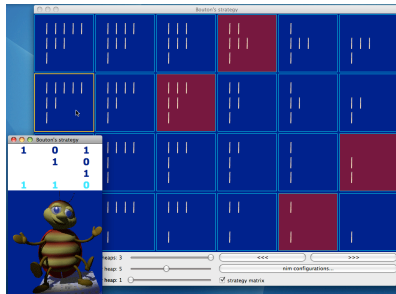
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History as meta-knowledge

- *Signs*: retaining information outside the human mind
data vs. information; nature, structure and scope of codes. . .
- *Rules*: disclosing new information outside the mind
formal treatment and artifacts; amenability to manipulation. . .
- *Mechanisms*: processing information outside the mind
informational perspective; automation of simple tasks. . .
- *Programs*: controlling plan-execution outside the mind
introspection and verbalization of algorithmic tasks. . .
- *Programs-as-data*: abstraction outside the mind
universal machine; abstraction levels and forms. . .
- *Complex systems*: intelligence outside the human mind?
management of complexity; toward artificial intelligence. . .

Signs & rules: Elementary school level

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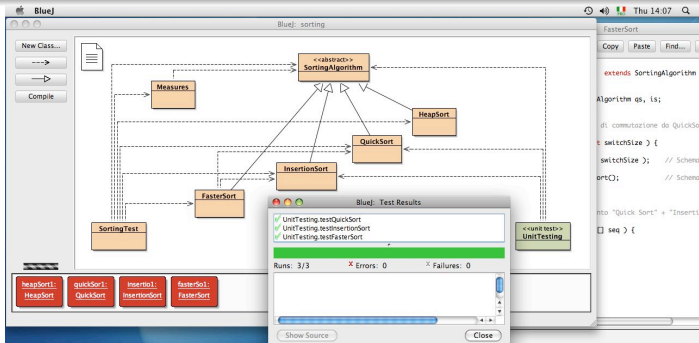




Rules, Mechanisms & Programs: Middle school level

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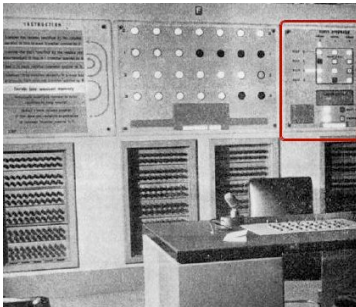
Later...



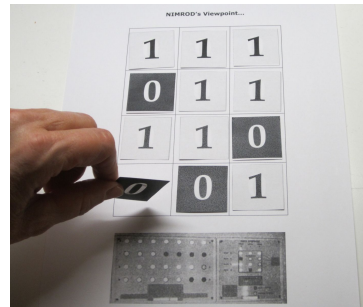
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Rules: ... “amenability to manipulation”

Nimrod

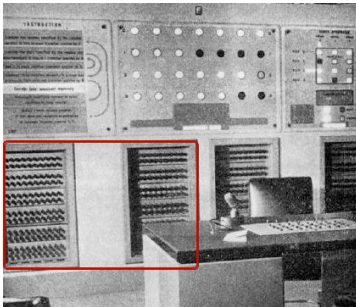


Unplugged



Mechanisms: ... automation of tasks

Nimrod

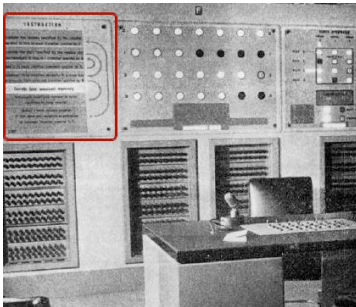


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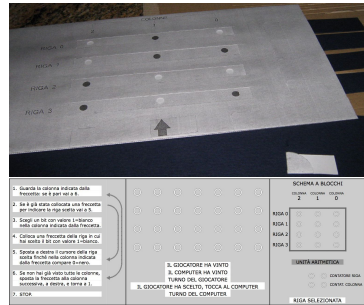


Programs: ... algorithmic procedures

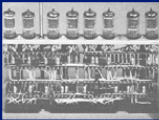

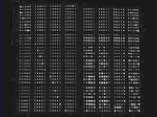

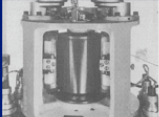



Nimrod



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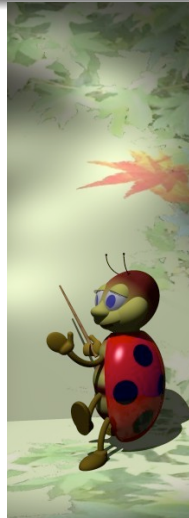


Contingent technologies vs. stable principles

	1 ms		10 ns
1 KB		50 MB	
	100 KB		1 GB
30 m³		60 cm³	

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Experience

- A few figures:
 - 5 teachers and 138 children of three middle schools
 - Larger program with 4 classes in s.y. 2011–12 (83 sixth-graders, age 11–12) and 2012–13
 - Core module with further 3 classes in s.y. 2010–11 (+ P4C; 33 eighth-graders) and 2012–13 (33 seventh-graders)
- Feedback:
 - From pupils: direct observation, questionnaires, exercises, tests
 - From teachers: meetings, PLS questionnaire



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What kind of feedback from pupils?

- Not yet sufficient for a full assessment of the impact on pupils' attitudes toward the sphere of computing
- But, it may tell us something about the achievement of particular objectives:
 - *engagement*
 - *appropriateness*
 - *topics of interest*
 - *outreach*



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Engagement

Quite high engagement. . .

- General project survey (PLS):
 - the overall experience was *worth doing* (> 90% of positive answers)
 - the themes were *interesting* (> 90% of positive answers)
- Specific perception questionnaire:
 - every kind of activity was *meaningful* to several (> 1/4) pupils
- Direct observation!



Appropriateness

Mostly appropriate for the age range. . .

- General project survey (PLS):
 - a few pupils (about 1/3) found some difficulties
 - . . . but teachers clear and material adequate (> 90% of positive answers)

- The teachers think so



Topics of interest

Several themes turned out to be appealing

- Perception questionnaire (*open* answers):
 - computing history
 - technological change
 - structure and potential of computers

- Interactions with researcher and teachers



Outreach

Maybe some outreach potential?

- Perception questionnaire:
 - Most pupils report having changed their view of *informatics* (2/3 vs. 1/5 of mathematics)
 - Interesting spontaneous questions:
 - “Why computers do not make errors?”*
 - “How is it possible to attain such a high density of integration in the digital devices?”*
 - “Which are the future perspectives of computing?”*



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Content-specific issues

- Review tests:
 - about 2/3 of the pupils master Bouton's strategy
 - as well as Nimrod's dataset
 - ... but about half the pupils are unable to follow a *precise* sequence of algorithm steps
- Investigation of nim variants and strategies (questionnaire):
 - apparently difficult for middle-schoolers
- More figures in the paper...



Competence issues

Competences attained in the formal operational stage may not yet be well developed:

- systematic case analysis
- understanding of transformations of transformations
- verbalization and precise description of a procedural task

Re-designing some tasks?



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Peculiar activities

- *Nim player imitation game*
 - not easy to see if the opponent is the computer!
 - a computer should play faster and better. . .
- *Surprising power of bit manipulation (Josephus problem)*
 - . . . and surprising findings by a couple of girls
- *Bird's-eye view of a general procedure*
 - how not to get lost while enumerating the configurations?
- *A bit of philosophy (P4C)*
 - appropriate for 8th-graders
who are constructing their identity
 - interesting links with Turing's seminal paper. . .



Teachers' feedback

From:

- Discussions during the meetings
- PLS anonymous questionnaire

Above all: they are working enthusiastically



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Conclusions

Gratifying experience:

- Seems to have been beneficial to pupils:
high engagement in the proposed tasks. . .
- . . . But also to the teachers:
different view of “informatics”
- Still work in progress. . .
- It would be interesting to study appropriate instruments
to assess the program from an edu-research perspective



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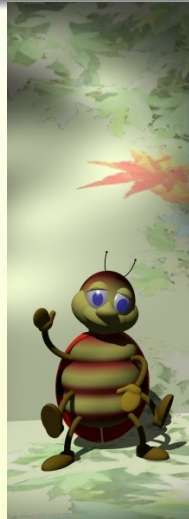


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Thanks for your patience. . .



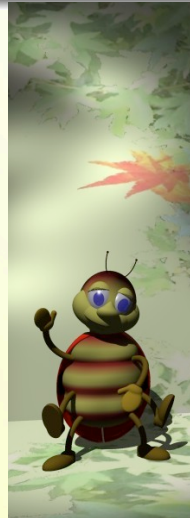
Thanks for your patience. . .

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